

A computational simulation of long-term synaptic potentiation inducing protocol processes with model of CA3 hippocampal microcircuit

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An experimental study of computational model of the CA3 region presents cognitive and behavioural functions the hippocampus. The main property of the CA3 region is plastic recurrent connectivity, where the connections allow it to behave as an auto-associative memory. The computer simulations showed that CA3 model performs efficient long-term synaptic potentiation (LTP) induction and high rate of sub-millisecond coincidence detection. Average frequency of the CA3 pyramidal cells model was substantially higher in simulations with LTP induction protocol than without the LTP. The entropy of pyramidal cells with LTP seemed to be significantly higher than without LTP induction protocol ($p = 0.0001$). There was depression of entropy, which was caused by an increase of forgetting coefficient in pyramidal cells simulations without LTP ($R = -0.88$, $p = 0.0008$), whereas such correlation did not appear in LTP simulation ($p = 0.4458$). Our model of CA3 hippocampal formation microcircuit biologically inspired lets you understand neurophysiologic data. (Folia Morphol 2018; 77, 2: 210–220)

Key words: learning and memory, hippocampus, long-term synaptic potentiation, forgetting, theta rhythm, computer simulation

INTRODUCTION

The modular structure of hippocampus may lead to a hypothesis that every area subserves specific computational functions, which results in development of various theories about the function of each subfield [52]. The CA3 area is believed to act as an auto-associative memory; however, DG's main take is probably producing internal representations which are infrequent and orthogonal.

Models of associative memory mostly rely on auto-associative networks [57] and discrete attractors ones, examples of which may include Marr [23] and McClelland et al. [24], Treves and Rolls [52], O'Reilly and McClelland [35], Hasselmo

et al. [15] and Shastri [44]. On the contrary, models for spatial learning are typically based on continuous attractor networks used to reconstruct experimental outcomes such as place field information [3, 9, 18, 41].

Misják et al. [26] introduced examples of hippocampal standardised models associated with spatial and episodic type of memory. They used a rate unit to evolve a model for the CA3 and thankfully to the Bienenstock et al. [5] learning rule, they could expose place cell properties, which can be used for preserving episodic memories. Rolls et al. [38] improved the model based on a consolidated attractor network. They were also using rate units, which are able to reserve both discrete and continuous representa-

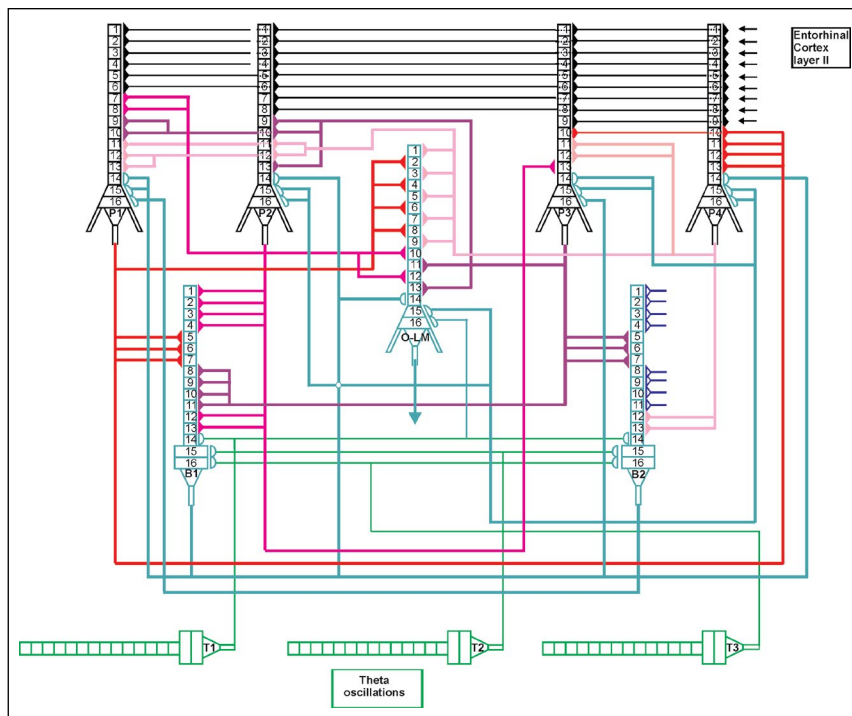


Figure 1. Hippocampal formation CA3 microcircuit showing pyramidal, basket and OL-M cells. CA1 network: P1, P2, P3, P4 — pyramidal cells; B1, B2 — basket cells and OL-M cell. Each CA3 pyramidal cell received excitation from the layer 2 entorhinal cortex.

tions. There are even more teams working on a “Spiking Model of Hippocampus for Guiding Behaviour” project, like Hasslemo’s, Eichenbaum’s and Robert Cannon’s group [13].

It has been proved that mossy fibres demonstrate a variety of long-term synaptic vividness containing asocional and N-methyl-D-aspartate (NMDA) independent form of long-term depression and potentiation (LTD and LTP) [6]. However, experiments with rats in which mossy fibres LTP/LTD were eliminated, provided no valid effects on learning task performance [54].

Hippocampal morphology — CA3 region

Pyramidal neurons are prominent cells in CA3 region and their population in a human brain is about 230×104 and 160×103 in a rat brain [7, 47]. Pyramidal cells accept excitatory inputs from perforate path in layer II of entorhinal cortex (4000 synapses), mossy fibres from dentate gyrus (50 synapses) and recurrent connections from CA3 (12,000 synapses) [54]. Action potentials generated in the CA3 are expanded to CA1 area through the Schaffer collaterals. The only sizable connection to other subcortical areas is the bilateral connection to the lateral septal nucleus [51]. The presence of this projection suggests that the lateral septal nucleus takes part in process of

learning and recall connected with CA3 associative memory model [15].

MATERIALS AND METHODS

The model describing simulation of CA3 microcircuit is presented in Figure 1. The model is built with various cell types which morphology includes the soma, axon and both apical and basal dendrites. There are four pyramidal cells (P1, P2, P3, P4), two basket cells (B1, B2) and one O-LM cell. The theta oscillation is delivered by the septo-hippocampal pathway and should be described as a frequency on the band of 4 Hz to 12 Hz [2, 25, 36, 37, 42, 43] and might be temporarily anchored in faster gamma-frequency oscillations [8, 10, 12, 50]. It is believed that this oscillation plays a basic role in hippocampal activity such as introduction of spatial information [34, 46], in-time locking cell activities and regulation of learning facilities [11, 16]. All mathematical specifications of CA3 model neurons are given in APPENDIX.

CA3 pyramidal cells

Every CA3 pyramidal cell consists of 16 compartments. Every dendrite has a synapse, an excitatory or inhibitory one. There are glutamate receptors for excitatory inputs: AMPA – E (k,i), NMDA – M (k,i).

GABA receptors are for inhibitory inputs: $I(k,i)$ where “ k ” is the number of dendrite compartments and “ i ” is a number of the area register table. Each CA3 cell receives somatic synaptic inhibition from CA3 basket cells in their somas and from the CA3 O-LM cells in their stratum lucid dendrites. Excitatory inputs in stratum lucid dendrites are received from CA3 pyramidal cells, layer 2 entorhinal cortex and dentate gyrus.

CA3 basket cells

Every CA3 basket cell consists of 16 compartments. Every dendrite has a synapse, an excitatory or inhibitory one. There are glutamate receptors for excitatory inputs: AMPA – $E(k,i)$, NMDA – $M(k,i)$. GABA receptors are for inhibitory inputs: $I(k,i)$ where “ k ” is the number of dendrite compartments and “ i ” is a number of the area register table. Excitatory connections are received to their distal dendrites from layer 2 entorhinal cortex and to medium dendrites from dentate gyrus granule cells mossy fibres. Inhibitory impulses come from connections in medial septum of their somas.

CA3 O-LM cells

In the CA3 region every O-LM cell consists of 16 compartments. Every dendrite has a synapse, an excitatory or inhibitory one. There are glutamate receptors for excitatory inputs: AMPA – $E(k,i)$, NMDA – $M(k,i)$. GABA receptors are for inhibitory inputs: $I(k,i)$ while “ k ” is the number of dendrite compartments and “ i ” is a number of the area register table. Each O-LM cell receives excitatory and inhibitory connections. The first ones are received from the active CA3 pyramidal cells in their basal dendrites, whereas the second one is received from the medial septum.

Hippocampal CA3 simulation environment

According to Witter [see 14] the CA3 area receives inputs from entorhinal cortex layer 2 and this input for every pyramidal cell was measured as firing at a medium frequency of 42 Hz. Each basket cell acquires input from entorhinal cortex layer 3 and dentate gyrus and a frequency of 50 Hz was modelled as the firing in this case. The firing average frequency for the medial septum was calculated as 8 Hz.

Synaptic properties

There are glutamate receptors for excitatory inputs: AMPA – $E(k,i)$, NMDA – $M(k,i)$. GABA receptors are for inhibitory inputs: $I(k,i)$ where “ k ” is the number of dendrite compartments and “ i ” a number

of the area register table. Each area simulates 0.5 ms of early time and primitively is filled with the resting potential of value $ReP = -80$ mV. The actual value of postsynaptic potential is estimated by using (Eq. 2.12) and (Eq. 2.13), for subsequent computations from (Eq. 2.14) and (Eq. 2.15–2.17). The so called spine coincidence detector for weight changes relies on the biological mechanism of the long-term synaptic potentiation (LTP) is in the dotted circle. AMPA and NMDA are both sorts of biological receptors. Ex means excitatory, Inh — inhibitory and PSP is summarised postsynaptic potential, measured as a disparity between the sums of Ex and Inh (see APPENDIX).

RESULTS

Biologically acceptable frequencies for all input strikes were chosen on the same principles as in the papers of Bliss and Lømo [6]. The excitatory inputs which originate in the modelled mossy fibres from dentate area; 7, 8 and 9 of CA3 pyramidal cells for LTP induction were stimulated at an average frequency of 100 Hz for 400 ms. There is a similarity between this examination and the one carried out by Bliss and Lømo [6] on the perforant path. The outcome of this experiment is a proof for biological plausibility of CA3 model as a mechanism related to processing of information. Figures 2 and 3 describe simulations accomplished with forgetting coefficient (FQ) from 10 to 100. Those simulations present correlation between increased FQ and output strike-trains. The value of LTP and frequency of action-potential generation enhanced in every examined case.

In the experiments carried out with and without the LTP inducing protocol after 10 s of stimulation it was observed that the average frequency decreased the pyramidal cells however the FQ has increased. This phenomenon could lead to a conclusion that the LTP induction facilitates the additional firing in correspondence with less valid input frequencies.

Average frequency of the CA3 pyramidal cells model was substantially higher in simulations with LTP induction protocol than without LTP ($p = 0.0001$). Very similar results were achieved for both basket and OL-M cells; indeed higher frequency ($p = 0.0001$) was observed in LTP induction protocol (Fig. 2).

The CA3 model was also examined without LTP inducing protocol and no frequency increase was proved after the 3rd second of simulation. Without LTP cells did not fire any action potential, even if the increase at the end of the 2nd second appeared.

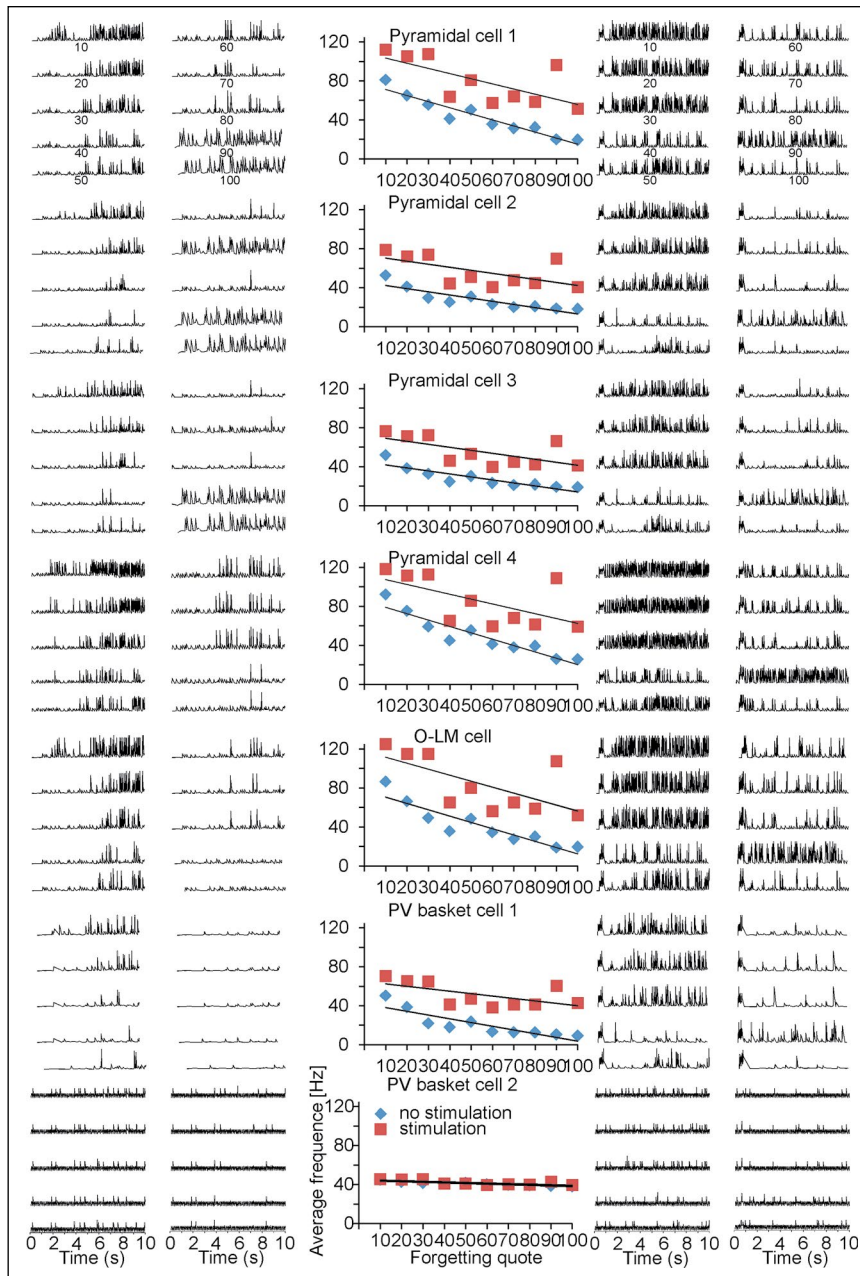


Figure 2. Basic 10 s real time simulation of pyramidal cells, basket cells and OL-M cell without and with long-term synaptic potentiation (LTP) inducing protocol. On the left: time course of summarised post-synaptic potential for all cells of CA3 region without LTP inducing protocol. On the right: time course of summarised post-synaptic potential for all cells of CA3 region with LTP inducing protocol. In the middle panel: correlations between forgetting coefficient 10, 20, 30, 40, 50, 60, 70, 80, 90 and 100 and average frequency for all modelled cells of CA3 region.

The trial without inducing LTP protocol in CA3 model presents that after 2-s duration of the experiment the increased pyramidal cells frequency stabilises at the value of 36.69 (1.80 Hz), which is very close to the most important input frequency 37.03 (1.03 Hz) planned for excitatory inputs of pyramidal cells.

The trial with inducing LTP protocol CA3 model presents that after 2-s duration of the experiment

the increased pyramidal cells frequency stabilises at the value of 53.75 (3.44 Hz) which is very close to the most important input frequency 57.75 (4.12 Hz) programmed for excitatory inputs of pyramidal cells (Fig. 3).

This experiment describes a huge diversification and higher quality for coincidence detection in simulation involving LTP induction protocol. In all cases the

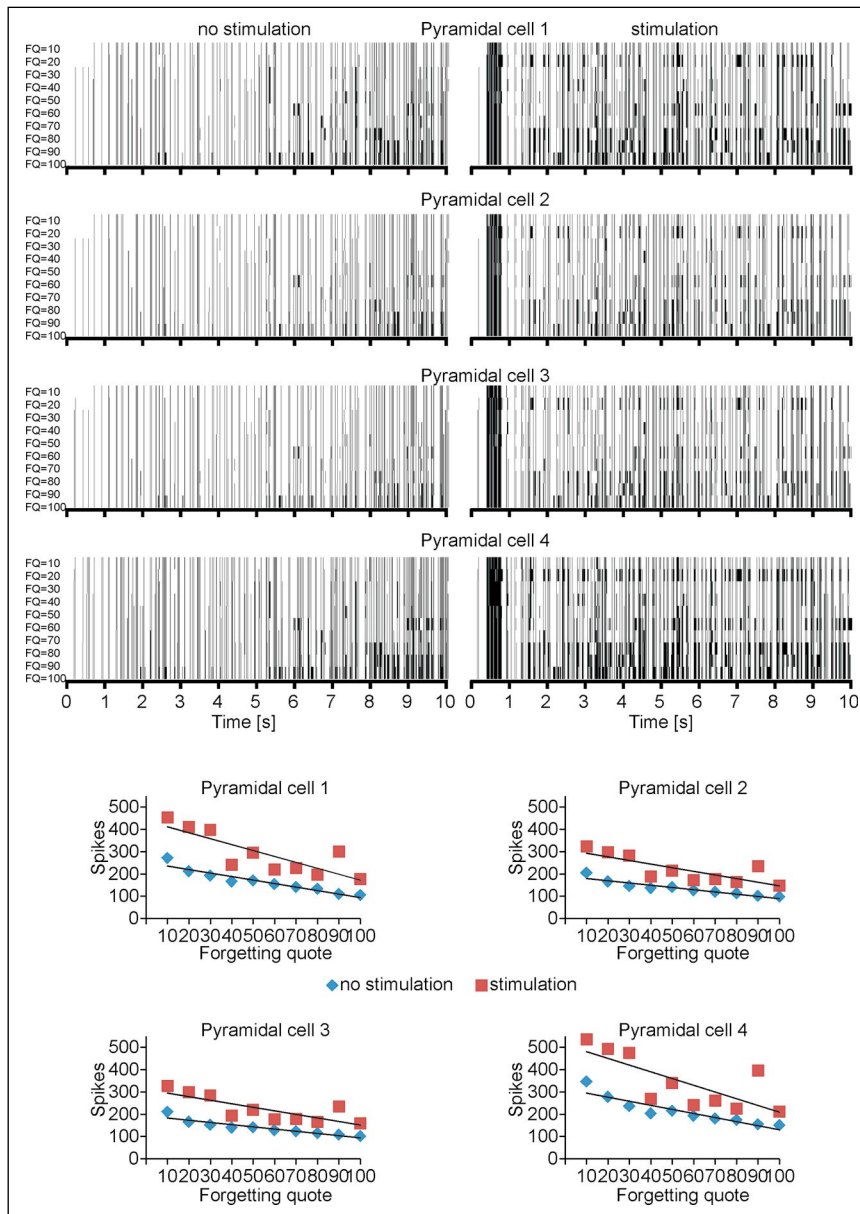


Figure 3. Basic 10 s real time simulation output spikes train of pyramidal cells, basket cells and OL-M cell without and with long-term synaptic potentiation (LTP) inducing protocol. On the left: output spikes train for all cells of CA1 region without LTP inducing protocol. On the right: output spikes train for all cells of CA1 region with LTP inducing protocol. On the bottom: correlations between forgetting coefficient 10, 20, 30, 40, 50, 60, 70, 80, 90 and 100 and number output spikes for pyramidal cells of CA3 region without and with LTP inducing protocol.

values of LTP enhanced after the training procedure. This occurrence was observed even within the nearby synapses of pyramidal cells in connection to those which were stimulated.

A diversity of methods can be used in order to present a regular or chaotic behaviour of CA3 model and multiple neural spike train data analysis. In this paper we present the visual recurrence analysis (VRA) which was expanded by Eugene Kononov and selected from a variety of methods. The results, which

are given in Figures 4 and 5, were accomplished with the forgetting coefficient 10, 20, 30, 40, 50, 60, 70, 80, 90 and 100. Moreover, Figure 4 describes relationship settling dimension, correlation dimension and entropy with forgetting quote with and without LTP inducing protocol.

There were no statistical differences in embedding dimension between simulation with LTP inducing protocols and without LTP ($p = 0.5668$) for pyramidal cells (Fig. 5). Similar outcome was achieved for

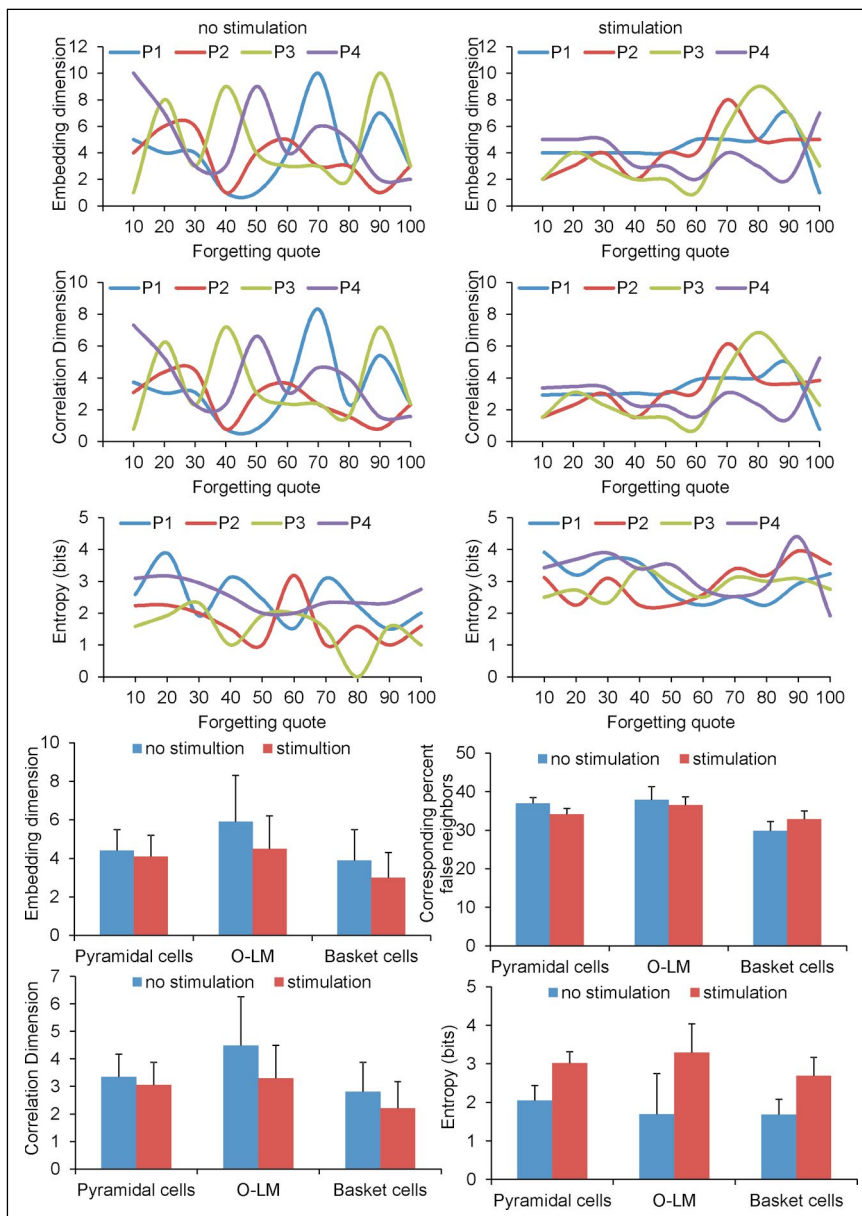


Figure 4. The recurrence result: embedding dimension, correlation dimension and entropy depending on the forgetting coefficient 10, 20, 30, 40, 50, 60, 70, 80, 90 and 100 of pyramidal cells without and with long-term synaptic potentiation (LTP) inducing protocol. On the left: results without LTP inducing protocol. On the right: results with LTP inducing protocol. Histograms on the bottom show comparison embedding with regard to dimension, correlation dimension, corresponding per cent of false neighbours and entropy without and with LTP inducing protocol.

correlation dimension ($p = 0.3447$; Fig. 4). However, the entropy of pyramidal cells with LTP seemed to be significantly higher ($p = 0.0008$; Fig. 5).

In case of basket cells there was no statistical significance among embedding dimension ($p = 0.2048$) and correlation dimension ($p = 0.1859$) conducted with and without LTP inducing protocol. The basket cell's entropy with LTP seemed to be significantly higher ($p = 0.0008$). Examined OL-M cells presented

statistical difference only for entropy, which was higher with LTP inducing protocol ($p = 0.0019$).

Results of simulation carried out with and without LTP inducing protocol proved that there is a strong interdependence among embedding dimension and correlation dimension ($p = 0.0001$).

There was depression of entropy, which was caused by an increase of FQ in pyramidal cells simulations without LTP ($R = -0.88$, $p = 0.0008$), whereas such cor-

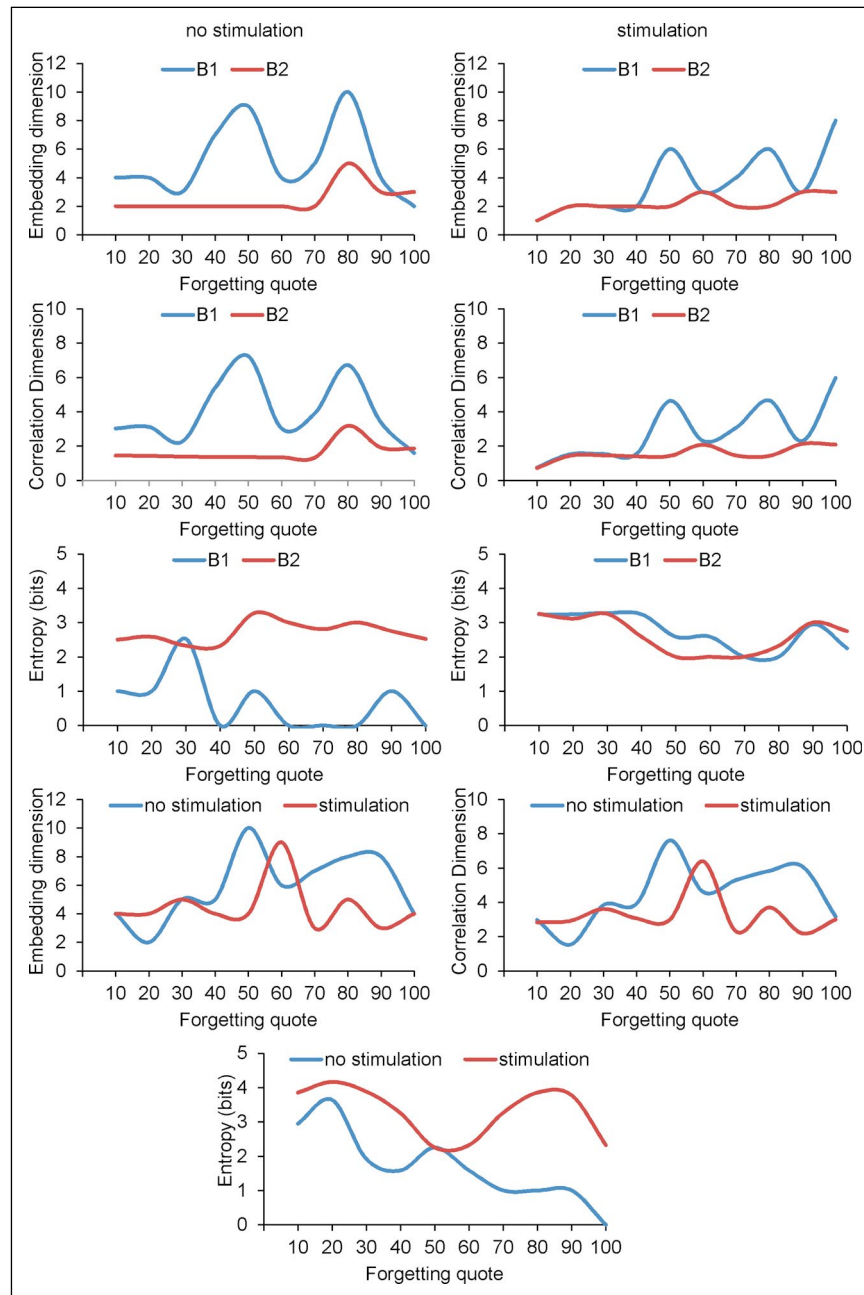


Figure 5. The recurrence result: embedding dimension, correlation dimension and entropy depending on the forgetting coefficient 10, 20, 30, 40, 50, 60, 70, 80, 90 and 100 of basket and OL-M cells without and with long-term synaptic potentiation (LTP) inducing protocol. The 3 diagrams on the bottom show comparison of the results obtained without and with LTP inducing protocol for OL-M cell.

relation did not appear in LTP simulation ($p = 0.4458$). The same phenomenon occurred in simulation with OL-M cells. Decrease of entropy was caused by FQ increase ($R = -0.93$, $p = 0.0001$), whereas such correlation did not appear in LTP simulation ($p = 0.1774$). However, in case of basket cells in LTP simulation the embedding dimension ($R = 0.85$, $p = 0.0020$) and correlation dimension ($R = 0.84$, $p = 0.0022$) increase were related to the increase of FQ.

Such correlation for basket cells did not appear in simulation without LTP inducing protocol ($p = 0.6329$; Figs. 4, 5).

DISCUSSION

The biologically plausible modelling of learning and memory in CA3 microcircuit has been presented. CA3 formation microcircuit acts also in a manner as auto-associative memory [39, 40].

Our stimulation is closely similar to the LTP-inducing protocols from the work of Bliss and Lømo [6], which describes how the short 100 Hz stimulation of perforant path in rabbit hippocampus can cause LTP on dentate granule cells. The presented model of CA3 hippocampal formation simulates the influence of the synaptic weights in pyramidal cells and timing of firing of different cells due to the theta rhythm in the same way as presented in [19, 20, 27, 48, 49, 53, 55]. We showed in our model CA3 network that excitatory and inhibitory cells modulate their output frequencies according to theta rhythm fired in phase with the trough of entorhinal cortex [14, 53, 55].

If an action potential reaches the synapse in the hippocampus and the subsynaptic region is depolarized enough, does the calcium ions influx begin immediately and cause LTP. It is commonly believed that such synaptic modifications are involved in memory and learning processes [1, 17, 22, 28–33, 56]. The basic mechanism for long-term potentiation induction to synapses is the calcium ions influx throughout NMDA channels [23, 35, 52, 57]. Such an ionic influx can occur only after removal of magnesium ions blockade of the NMDA channel by enough depolarisation of postsynaptic region. An instant depolarisation of the subsynaptic region depends on the history of inputs patterns, and so any accessory input in any form or shape could potentially enhance the ability to learn. It could be considered as a remote equivalent of the stochastic resonance phenomenon. As a cardinal mechanism involved in the learning process within the nervous tissue, the above should be employed in every complex or simplified neuronal model.

CONCLUSIONS

The most contemporary interest of medicine is a detailed explanation of course and possibilities for diagnosis and treatment of Alzheimer disease which cause at the late stage complete loss of contemporary memories [21]. And the hippocampo-entorhinal connections are crucial for this disease. At the late end stage the perforant path is completely destroyed. In initial stages, only a few out of thousands of connections from layer 2 stellate cells of entorhinal cortex are disrupted but it always leads to diminished possibilities for learning and memorisation of new cues. And such phenomenon could be easy modelled in presented circuit with enhanced FQ.

In presented circuit we use to model nonlinear dynamic systems an alternative approach to the tra-

ditional differential equations. Our presented nonlinear methods are universal and could be used with any binarised time series of data, i.e. for evaluation of changes in heart rhythm [4]. The CA3 model allows modifications of some parameters from various functions and the changing of the cable properties of the dendrite with LSW values. We can also modify input functions so that they collaborate with the receptors in a way as ribbon synapse and use the pyramidal cell of CA3 region for the modelling of ganglion cells [45].

APPENDIX

Neuronal models of CA3 equations and parameters

The programme clock step of the presented model equals 0.5 ms of the simulated real time. First we create tables of shift registers; they form an array of looking up buffer tables. For excitatory inputs (glutamate receptors): AMPA – E (k,i), NMDA – M (k,i), and for inhibitory inputs (GABA receptors): I(k,i) whereas “k” is the number of the dendritic compartment, “i” is a number of an area in a particular register table.

Synaptic function — SF(t) calculates, after the arrival of an action potential on a particular synapse, the typical time courses of excitatory or inhibitory postsynaptic potentials (EPSP or IPSP) and furthermore adjusted in term of parameters calculated from functions: Adaptation (2.2) and Memory (2.6) to the appropriate register table. It could be in simply linear form (2.1), but other forms as double exponential alpha function are also possible for use.

$$SF(t) = \begin{cases} 0 & t = t_{sd} \\ \frac{A_{MAX}}{t_r} (t - t_{sd}) & t_{sd} < t \leq t_r \\ \frac{A_{MAX}}{t_d} [(t_d - (t - (t_r + t_{sd})))] & t_r < t \leq t_d \end{cases} \quad (2.1)$$

Where: t_{sd} — time of synaptic delay, t_r — time of EPSP/IPSP rise, t_d — time of EPSP/IPSP decay, 1 millisecond (ms) = 2 steps of i. Parameters for EPSP_{AMPA}: $A_{MAX} = 5$ mV, $t_{sd} = 1$ ms, $t_r = 2$ ms, $t_d = 13$ ms, for EPSP_{NMDA}: $A_{MAX} = 1$ mV, $t_{sd} = 1$ ms, $t_r = 2$ ms, $t_d = 13$ ms, and for IPSP_{GABA}: $A_{MAX} = -2.5$ mV, $t_{sd} = 1$ ms, $t_r = 2$ ms, $t_d = 10$ ms.

Adaptation — A(k,i) (for excitatory inputs):

$$A(k,i) = \frac{(ReP-Rsp)-(ReP-S(k, i))}{(ReP-Rsp)} \quad (2.2)$$

Where S(i) is the actual value of summarised potential in the k compartment, ReP and Rsp parameters.

ReP = -80 mV (resting potential value), Rsp = -10 mV (reverse synaptic potential). It presents the possibility of reverse ionic flow through the membrane channels according to the Nernst equation.

Weight of compartment k — W(k) (for excitatory inputs):

$$W(k) = \frac{1-LSW}{NE-1} (k-NE) + 1 \quad (2.3)$$

Where: LSW, NE — parameters; LSW (low significant weight) — weight of the most distal dendrite input. NE = 13 — a number of excitatory inputs. Thus within this function the cable properties of a modelled dendrite could be simply changed.

Function influence — Inf(a,b) of a compartment on b compartment (for excitatory inputs):

$$\text{Inf}(a, b) = \begin{cases} 1 - \frac{1-LSW}{(N-1)} (a-b) & b \geq a \\ 1 - \frac{4}{N} (a-b) & (a-b) \leq \frac{N}{4} \\ 0 & \text{otherwise} \end{cases} \quad (2.4)$$

N = total number of inputs and a, b ∈ N. This function allows for the calculation of summarised postsynaptic potential in a particular compartment (2.5) with respect to all others.

Summarised potential — S(k; i) in compartment k (for excitatory inputs):

$$S(k, i + 1) = \text{ReP} + \sum_{m=1}^{NE} (E(m, i) - \text{ReP}) \text{Inf}(m, k) \quad (2.5)$$

Where: NE — number of excitatory inputs, Inf(m,k) influence of m — compartment on k, E(m;0) the actual value of the appropriate register.

Long-term synaptic potentiation (LTP), called, in short, Memory (Mem):

If S(k,i) > CaMT then

$$\text{Mem}(k) = 1 + \ln \frac{C_k(i+1)}{6 \text{ clog}} \quad (2.6)$$

CaMT = -68 mV (threshold for the removal of the Mg ion block for NMDA channels), C(k; i) time of memory for compartment k, clog parameter = 2.3026. If we have simultaneously an action potential on excitatory input and opened NMDA channels due to enough depolarisation of the postsynaptic region (2.5), the LTP induction occurs; the weight of this synapse is being increased. Initiation of the cascade of biochemical reactions, those leading to LTP, depends of amount of calcium ions influenced throughout the opened NMDA channels.

We modelled the pnenomenological event by power function:

$$\text{power} = \text{powerA}(M(k;i) - \text{ReP}) \quad (2.7)$$

Whereas powerA = 9 is a parameter, M(k;i) — actual value of SF(i) for EPSP(NMDA) in appropriate register.

Time of memory duration C(k; i):

$$C(k, i + 1) = C(k, i) + e^{\text{power}} - 1 \quad (2.8)$$

Where: FQ; ReP — parameters. FQ — forgetting coefficient: it decreases, for the next simulation step, the calculated memory time of the programmed value. Clog, powerA, and FQ are numerical parameters, their changes allow confining the strength and time of LTP to biologically plausible values for any kind of modelled neuron.

Input function (InEx(k)) for excitatory and InInh(k) for inhibitory synapses adds, after the arrival of an action potential (input > 0), the values of the synaptic function (2.1) to the appropriate tables of shift registers E(k;i;t), M(k;i;t) and I(k;i;t), see below (2.9), (2.10) and (2.11). This sum is done with respect to the parameters calculated from functions (2.2) adaptation and (2.6) memory — LTP: thus the other functions are subsequently calculated and the threshold function is proofed.

$$E(k;i;t+1) = E(k;i;t) + A(k;i) \text{Mem}(k;i) \text{SF}(t) \quad (2.9)$$

$$M(k;i;t+1) = M(k;i;t) + \text{SF}(t) \quad (2.10)$$

$$I(k;i;t+1) = I(k;i;t) + \text{SF}(t) \quad (2.11)$$

Summarised postsynaptic potential in neuron (PSP):

$$\text{PSP}(i+1) = \text{ReP} + \sum_{m=1}^{NE} W(k)(E_{m,0}(i) - \text{ReP}) + \sum_{m=1}^{NE} I_{m,0}(i) - \text{ReP} \quad (2.12)$$

Where: W(k) — weight of compartment k, E(k;i), I(k;i) are the actual values of the tables from register E and I calculated with (2.9), (2.11), whereas the values of Adaptation (2.2) and Memory (2.6) are from a previous programme step. NE and NI are numbers of excitatory and inhibitory inputs. Threshold function for action potential: threshold = -50 mV:

$$\text{out} = \begin{cases} 0 & \text{PSP} \leq \text{threshold} \\ 1 & \text{PSP} \geq \text{threshold} \end{cases} \quad (2.13)$$

Refraction is modelled for the time up to 2 ms by a reset of PSP value (2.11) for inhibitory input registers I(k;i) to the resting potential and shifting the voltage in the register tables E(k;i) for excitatory inputs according to the:

$$\text{ADRV}(k) = \text{ReP} - \frac{(\text{ReP} - \text{RePB})(\text{NE} - k)}{\text{NE}} \quad (2.14)$$

ADRV — AntiDromic Reset Voltage function (2.14); RePB is a parameter — voltage to which the most distal dendrite compartment is resetting (−79 mV), ReP = −80 mV. NE — number of excitatory inputs.

Shifting of registers E; M; I; occurs at the end of each simulation step and the values in all registers tables are shifted as follow (th-threshold):

$$\forall_{k \in N} \forall_{i \in (0,31)} E_{k,i}(t+1) = \begin{cases} E_{k,i+1}(t), & \text{for PSP} < \text{Threshold} \\ \text{ReP}, & \text{for PSP} \geq \text{Threshold} \end{cases} \quad (2.15)$$

$$\forall_{k \in N} \forall_{i \in (0,31)} M_{k,i}(t+1) = \begin{cases} M_{k,i+1}(t), & \text{for PSP} < \text{Threshold} \\ \text{ReP}, & \text{for PSP} \geq \text{Threshold} \end{cases} \quad (2.16)$$

$$\forall_{k \in N} \forall_{i \in (0,31)} I_{k,i}(t+1) = \begin{cases} I_{k,i+1}(t), & \text{for PSP} < \text{Threshold} \\ I_{k,i}(t), & \text{for PSP} \geq \text{Threshold} \end{cases} \quad (2.17)$$

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