

# Automatic precise P-wave assessment

## Automatyczny precyzyjny pomiar załamka P

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### Abstract

**Introduction.** The electrophysiological activity of the heart is registered and presented in form of electrocardiogram (ECG). Precise P-wave measurement is crucial for a proper assessment of signal conduction inside the atria. For the sake of validating the precise manual measurements, the study team has created an automatic software customized for precise P-wave measurements (APPA, automatic precise P-wave assessment). The present study aims to prove that the automatic algorithm has a comparable efficiency in precise P-wave duration measurement.

**Material and methods.** The study group included 72 patients (31 males, 41 females) aged  $62.8 \pm 14.27$ , undergoing different electrophysiological procedures. The P-wave was measured twice: first, manually at the paper speed of 200 mm/s, 64–128× (precise), and second, automatically, with the use of APPA, which filters the signal every 1 millisecond.

**Results.** There are no statistical differences between manual and automatic measurements. The mean difference between the two methodologies is 3.72 ms. The median P-wave duration was negligibly higher for manual measurements in all types of arrhythmia. The biggest difference in measurements was present in patients with atrial fibrillation. The lowest difference was present at the range of 110–130 ms of the P-wave duration.

**Conclusions.** The measurements taken by APPA, and manually are equally precise, which supports the authors' previous results. Their algorithm presents high reliability of results and can be used for scientific purposes. The structural destruction of atria results in self-hiding of the actual duration of the P-waves in ECG. With higher precision of measurements, the differences between minimal and maximal duration of the P-waves in different leads decrease to negligible values.

Key words: P-wave duration, automatic algorithm, software, P-wave measurements

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### Introduction

The electrical activity of the working heart is presented in a form of a 12-lead electrocardiogram (ECG). The ECG signal is defined as depolarization i.e. the potential change from negative to positive which spreads across

the myocardium followed by depolarization. The activity of the atria is marked by the deflection called the P-wave. The depolarization results in forming up a deflection from the isoelectric line. If a vector is consistent with the direction of the bipolar lead or is oriented towards the unipolar lead, the deflection is positive. In the opposite situation,

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the deflection sets negatively. When the vector spreads perpendicularly to bipolar lead direction, or parallel in the case of unipolar leads, no deflections are being formed, which results in isoelectric fragments in ECG. Considering the complexity of the heart conduction system and its myocardial components, this never fully happens in practice, however, this fact helps to understand the presence of the flattened, irregular ECG fragments. After analysing the coordinates of the signal, it was found that the duration of the P-wave differs significantly from the one taken with less precise methodology [1, 2]. Despite more accurate assessment, the results and conclusions of this work were still doubted [3, 4]. To support the present findings, the team designed an original, specially calibrated automatic algorithm that analyses every millisecond of the recording. Precisely measured P-wave duration becomes highly useful in defining a total atrial activation time, essential for advanced diagnosis.

The study aimed to compare the manually taken P-wave duration measurements with the ones taken automatically in a wide, unselected population of patients with atrioventricular nodal reentrant tachycardia (AVNRT), atrial flutter (AFL) and atrial fibrillation (AF). The additional goal of this study is to prove that the P-wave durations are equal in different leads of the ECG, no matter the type of arrhythmia.

## Material and methods

Seventy-two patients (31 males, 41 females) aged  $62.8 \pm 14.27$  were included in the study. The patients were divided into 3 numerously equal (24 pts) subgroups dependent on the type of arrhythmia: AF, AFL, AVNRT. The measurements were taken twice within those subgroups: the first time manually, which is treated as a golden standard, and the second time automatically with the originally developed algorithm. The manual measurements were taken 3 times in all leads by 2 independent investigators unaware of the mutual results and clinical data of the patients. The LabSystem Pro electrophysiological system was used for the manual measurements, which allowed the use of parameters: 200 mm/s, magnification 64–128×. By using vector graphics, the researchers were able to zoom the record without any quality loss. The electrophysiological system allowed to analyse the record at the rate of 1 px/1 ms using a 4K TV as the screen. For automatic measurements, the team used the specially designed software – automatic precise P-wave assessment (APPA). The algorithm was calibrated to imitate the skills of most experienced human researchers and to keep the repeatability of the measurements. The signal was analysed every 1 millisecond, and the algorithm was set to detect the raise of the isoelectric line and define the beginning of the P-wave. In some cases, the quality of the recording was so distorted, that it was impossible for the algorithm to objectively detect the beginning of the P-wave, due to

the artifacts' overlap. However, such cases were excluded from the study, as the intention was to keep the results as objective as possible. The measurements were compared, contrasted and analysed between the subgroups. The construction of the algorithm results in a slight deviation of  $\pm 10$  ms in measurements. Due to small fluctuations of the isoelectric line, which occur in every case, the algorithm starts to calculate the beginning of the P-wave after 10 ms, if the determined condition is met. Similarly, the measurement ends after 10 ms when the termination condition is reached. Therefore, assuming that the algorithm may distort the measurement at the beginning and end on average by 5 ms, the statistical error was 10 ms. This can be easily supported by the probability theory, which proves that after e.g. 1 million random sampling attempts [real random numbers – the probability density function with a normal distribution  $N(0, \sigma^2)$ ] of numbers from 1 to 10, the mean is 5. Concluding from this, the error does not exceed 10 ms (5 ms at the beginning of the P-wave and 5ms at the end) [5, 6]. Taking a closer look at the errors, they can be divided into systematic, random and excessive. These types of errors are not considered, because in this case the examination concerns exactly one patient and his/her health condition during the examination. Moreover, the algorithm does not analyse the disturbed periods, marking them as damaged – it is not analysed why they occurred, they are just automatically rejected. Therefore it can be concluded that the only statistical error is 10 ms. Of course, there is a probability of achieving an error of 20 ms, but it is just as probable as the error of 0 ms (no error). From a mathematical point of view, for many respondents, the above-mentioned cases neutralize each other, although they may occur in separate cases. Most importantly, however, the present study relies on a series of studies which makes the measurements more objective from the statistical point of view.

## Statistical analysis

For quantitative variables, basic descriptive statistics were calculated (M – average, SD – standard deviation, Me – median, Q1 – lower quartile, Q3 – upper quartile, Min – minimum value, Max – maximum value), and the compliance of their distributions with theoretical normal distribution was checked using the Shapiro-Wilk's W test. Comparisons were performed with the Students' T-test or Mann-Whitney U test for independent groups or Kruskal-Wallis ANOVA for multiple comparisons. Each categorical variable was presented as numbers and percentages. The comparisons were performed with the Chi-square test. The correlations between studied parameters were performed using Pearson's correlation coefficient or Spearman's rank correlation coefficient according to the statistical properties of the data. The statistical analysis was performed using the computer program STATISTICA v.13.3 (StatSoft,

Inc., Tulsa, USA). P-values less than 0.05 were considered significant.

## Results

The clinical and demographic characteristics of the patients in the 3 study subgroups taking part in the present research are presented in Table 1. The data include age,

sex and comorbidities of the patients concerning 3 types of atrial arrhythmia.

Table 2 presents the statistical information about P-wave durations measured manually and automatically in 3 subgroups of atrial arrhythmias.

The longest results including mean, median and minimum-maximum values are present in the subgroup of AF, measured both manually and automatically. The shortest

**Table 1.** Clinical and demographic characteristics of the patients in the three study groups

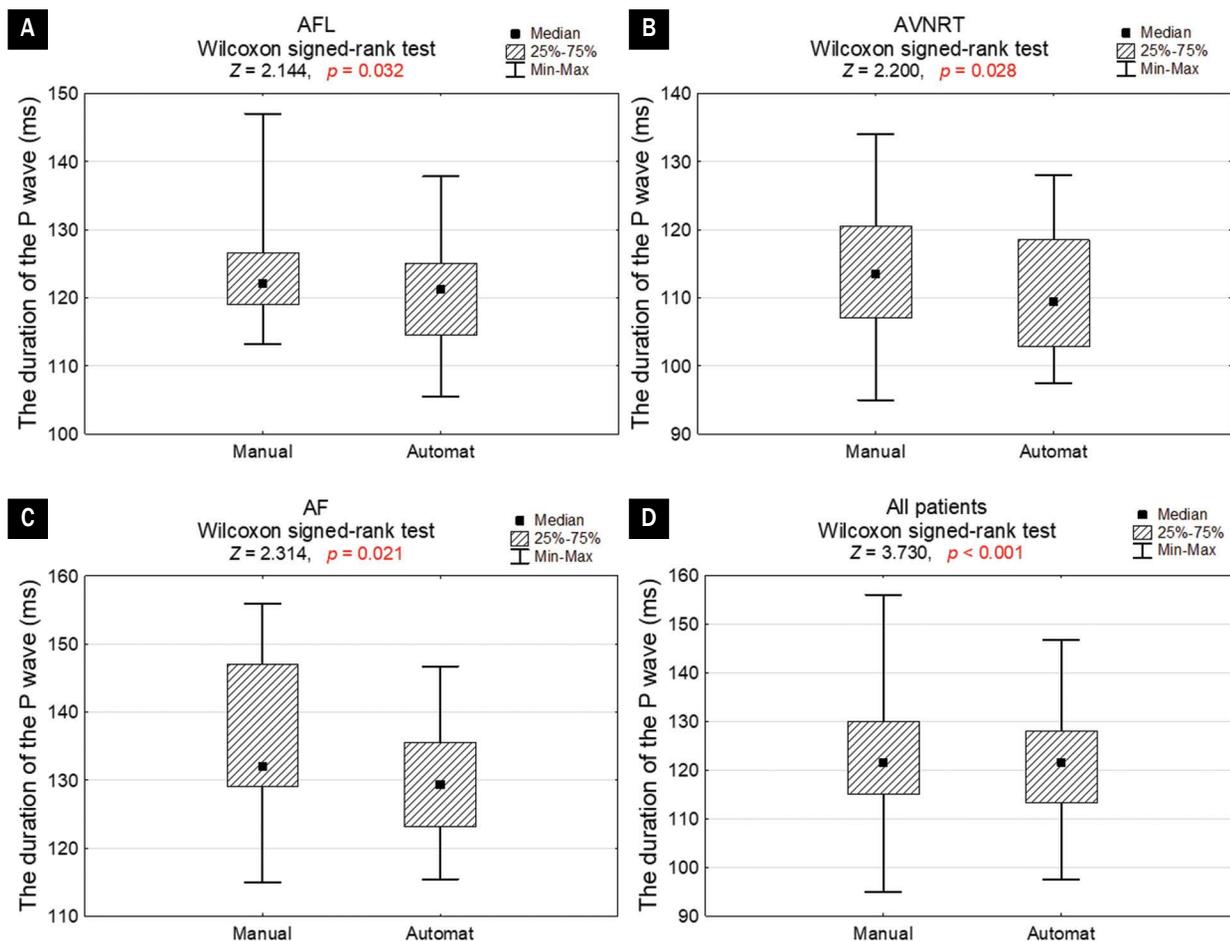
Variable	Group						P-value
	AVNRT n = 24		AFL n = 24		AF n = 24		
	n	%	n	%	n	%	
Sex							< 0.05
Women	20	27.78	10	13.89	11	15.28	
Men	4	5.56	14	19.4	13	18.06	
Comorbidities							< 0.05
HT	15	62.5	17	70.8	18	75.0	
DM	2	8.3	5	20.3	6	25.0	
CKD	2	8.3	3	12.5	2	8.3	
IHD	3	12.5	5	20.3	5	20.3	
HF	2	8.3	3	12.5	3	12.5	
Age (years)							< 0.01
Mean ± SD	55.3 ± 12.03		64.9 ± 12.38		68.3 ± 15.12		

AF – atrial fibrillation; AFL – atrial flutter; AVNRT – atrio-ventricular nodal re-entry tachycardia; CKD – chronic kidney disease; DM – diabetes mellitus; HF – heart failure; HT – hypertension; IHD – ischemic heart disease; SD – standard deviation

**Table 2.** Mean P-wave durations determined manually and automatically and the difference between them ( $d_{M-A}$ ) in patients with different types of atrial arrhythmia and the results of significance tests

	The duration of the P-wave [ms]			P-value
	Manual	Automat	dM-A	
AVNRT	n = 24	n = 24	n = 24	0.045
Mean ± SD	113.8 ± 9.8	110.6 ± 9.1	-3.2 ± 7.4	
Median (IQR)	114 (107-121)	109 (103-119)	-2 (1-6)	
Min-max	95-134	98-128	-29-7	
AFL	N = 24	N = 24	N = 24	0.032
Mean ± SD	123.4 ± 7.5	120.6 ± 8.1	-2.8 ± 7.8	
Median (IQR)	122 (119-127)	121 (115-125)	-5 (-7-3)	
Min-max	113-147	106-138	-25 -17	
AF	n = 24	n = 24	n = 24	0.021
Mean ± SD	134.9 ± 13.2	129.7 ± 8.0	-3.2 ± 7.4	
Median (IQR)	132 (129-147)	129 (123-136)	-2 (1-6)	
Min-max	115-156	115-147	-29-7	
All patients	n = 72	n = 72	n = 72	< 0.001
Mean ± SD	124.0 ± 13.5	120.3 ± 11.4	-3.4 ± 9.1	
Median (IQR)	122 (115-130)	122 (115-128)	-2 (1-8)	
Min-max	95-156	98-147	-30-20	

AF – atrial fibrillation; AFL – atrial flutter; AVNRT – atrio-ventricular nodal re-entry tachycardia; IQR – interquartile range; Max – maximum value; Min – minimum value; SD – standard deviation

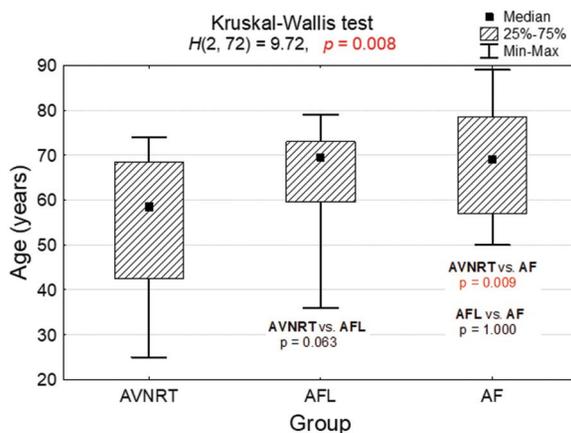


**Figure 1A–D.** The duration of the P-wave in the atrio-ventricular nodal re-entry tachycardia (AVNRT), atrial flutter (AFL), atrial fibrillation (AF) groups and the entire study group of patients were determined manually and automatically, and the results of significance tests; Max – maximum value; Min – minimum value

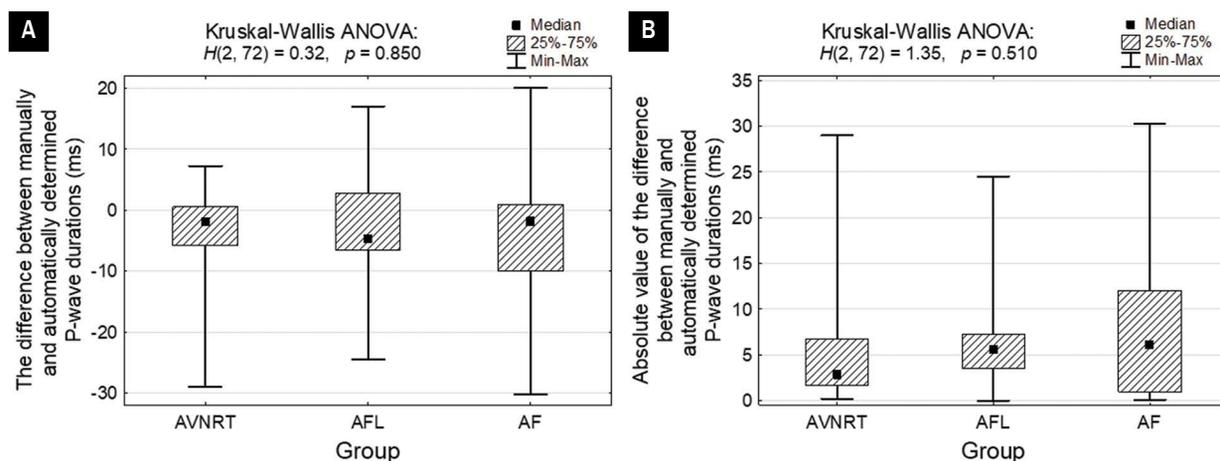
ones are present in the subgroup of AVNRT. The results are supported with a significance test.

Figure 1 presents the results of the significance Wilcoxon signed-rank test relating to the differences in duration of the P-wave in all patients and the groups of patients with AVNRT, AFL, AF. The median of the P-wave duration is slightly higher in the case of manual methodology, contrasting to the automatic measurement in the 3 subgroups separately. However, the significance test is  $p < 0.001$  for all patients analysed altogether regarding manual/automatic methodology.

Figure 2 presents the differences, relations and proportions of age in the studied groups of patients. The differences are analysed with the Kruskal-Wallis significance test, and post-hoc tests (Dunn’s tests) in 3 groups. It can be easily noticed that the subgroup of patients with AF is statistically the most advanced in age. This fact corresponds with the above-presented results of the longest P-wave



**Figure 2.** Age of the studied patients in groups differing in the type of atrial arrhythmia and the results of the Kruskal-Wallis significance test and post-hoc tests (Dunn’s tests); AF – atrial fibrillation; AFL – atrial flutter; AVNRT – atrio-ventricular nodal re-entry tachycardia; Max – maximum value; Min – minimum value



**Figure 3A, B.** Difference between P-wave duration in atrio-ventricular nodal re-entry tachycardia (AVNRT), atrial flutter (AFL), manual and automatic atrial fibrillation (AF) groups and significance test results; Max – maximum value; Min – minimum value

durations in the very same group. Similarly, the subgroup of patients with AVNRT is the youngest one, which corresponds with the shortest P-wave durations.

Figure 3 shows the difference, and the absolute value of the difference between manually and automatically measured P-wave durations in 3 study groups analysed with the Kruskal-Wallis ANOVA test.

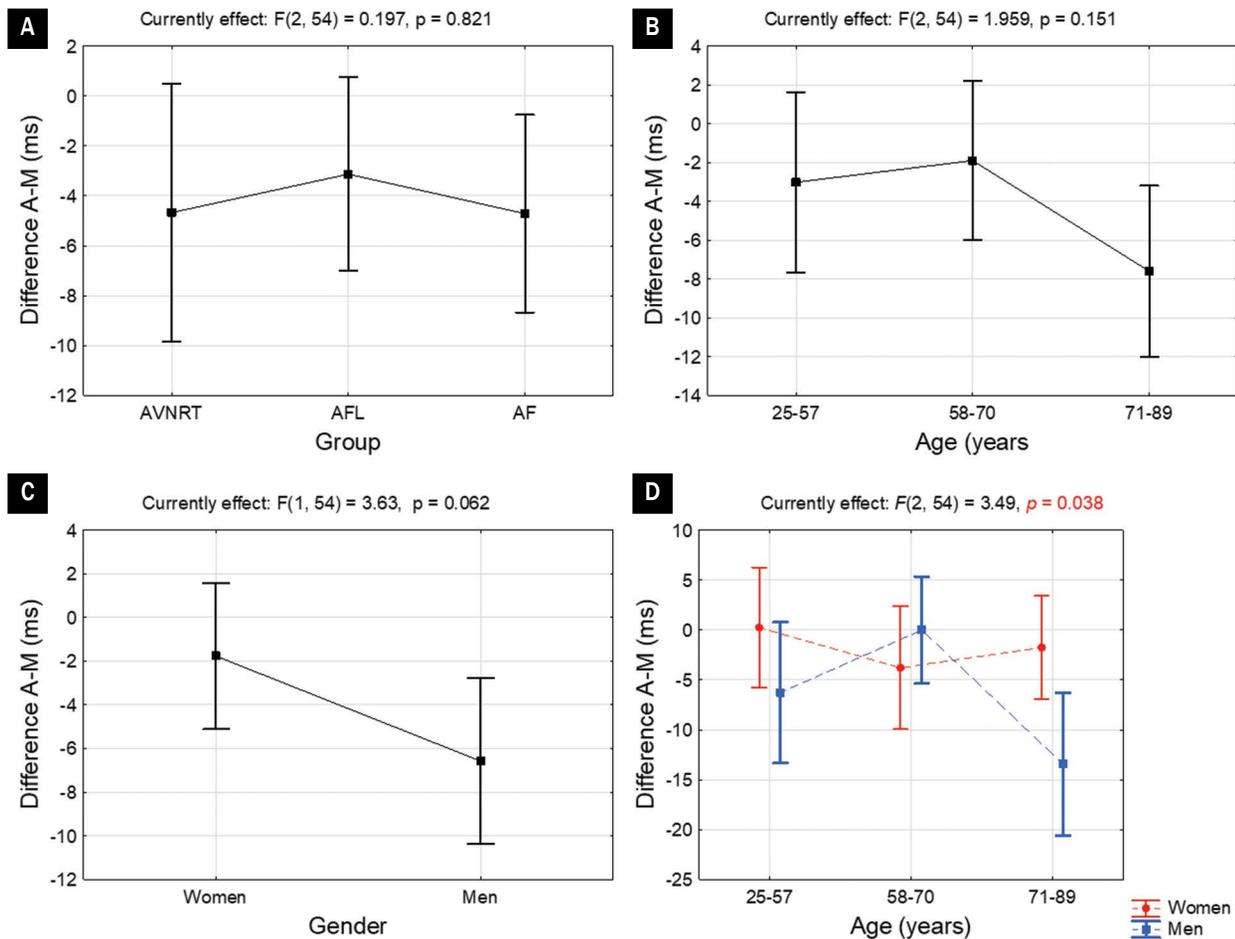
When it comes to the difference in milliseconds, it is noticed that the greatest range of 25–75% happened in the subgroup of AF, and slightly lower in AFL. In the subgroup of AVNRT however, the range of the difference was distinctly lower. The absolute value of the difference between manually and automatically determined P-wave duration was visibly bigger in the subgroup of AF, in contrast to AFL, AVNRT.

Figure 4 presents the graphical interpretation of the results of multivariate analysis concerning the difference between manual and automatic measurements in 3 study groups. The first couple of charts reveals a similar profile of the difference in measurements considering the type of arrhythmia and age. The difference between manual and automatic measurements is higher in men considering the whole study group. The difference between manual and automatic measurements is close to 0 for women and men in the groups of age respectively: 25–57, 58–70 years old.

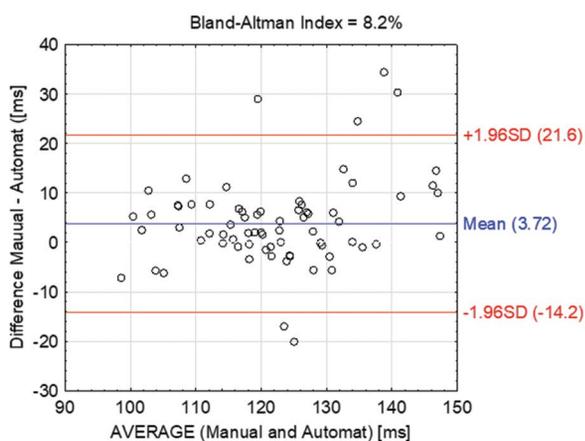
Figure 5 represents the Bland-Altman Index and Bland-Altman plot showing the relation between the differences of the P-wave durations taken manually and automatically, and the average duration of the P-wave. The mean difference between manual and automatic measurement methodology is 3.72 ms, and the highest density of the results is included between 110–130 ms.

## Discussion

The most important achievement of this research is the fact that APPA has proven similar effectiveness and precision in measuring the P-wave duration to an experienced researcher. This fact means that the results of this research based on manual measurements are not disturbed by the subjectivism of the researchers [7, 8]. The accurate duration of the P-wave is an essential substrate for calculating a total atrial activation time, which can be used as a predictive factor for AF. In the following discussion, the study findings are analysed, and the methodology is confronted with the others in use since 1997. The most fundamental principle of electrocardiography is the fact that all electrophysiological phenomena begin and end at the same time and place, regardless of the lead. Different leads should be treated as different perspectives of observing the same signal repeatedly. This is logical and based on the physical properties of electric signals spreading in space and time. Nevertheless, in 1997, Dilaveris [9] introduced the concept of P-wave dispersion as the difference between the longest and shortest P-waves in two different leads, assuming wrongly, that this case happens at all. The duration of P-waves was determined using a ruler, a magnifying glass, and ECG recording at the paper speed of 50 mm/s and the feature of 1 mV/cm. The maximum P-wave duration of 110 ms and dispersion of 40 ms were positive predictive values of 89%. The dispersion in the study group was  $49 \pm$  ms and in the control group  $28 \pm$  ms, which was statistically significant. In the following years, the P-wave dispersion became a popular parameter, which resulted in the creation of many scientific papers based on incorrect, still copied



**Figure 4A-D.** Graphical interpretation of the results of multivariate analysis of variance for the difference between the duration of the P-wave in a group of 72 patients of different sex, age and type of atrial arrhythmia



**Figure 5.** Bland-Altman plot for manually and automatically determined P-wave duration and the value of the B-A index

methodology [10, 11]. The results of research based on the opposite methodology were presented in 2015 at the Europace conference by the team of Zimmer et al. [12]. The authors took the measurements for the first time with the settings: 50 mm/s, 8 $\times$ ; and the other time with more accurate settings: 200 mm/s, 128-256 $\times$ . For this purpose, they used the properties of vector graphics, contrary to the measurements taken by Dilaveris, who used raster graphics. The results revealed that with less precise settings the dispersion was 45.14 ms, while with more precise settings it was 1.24 ms, so it practically disappeared. The results also showed a direct correlation of Pmax/Pdisp, which meant that dispersion couldn't be an independent parameter. The confirmation of this discovery was the work published in 2020 [12]. Using the methodology of Zimmer [12], the P-wave dispersion

was:  $44.1 \pm 16.8$  ms (50 mm/s, 8×), and  $2.8 \pm 3.4$  ms (200 mm/s, 64–128×). The particularly interesting phenomenon occurred in the work of Yamada et al. [13], who published his results only two years after Dilaveris had introduced the theory of the P-wave dispersion. The author used automatic software for the measurements and the P-wave dispersion was on average  $26.6 \pm 9.5$  ms in the study group and  $14.8 \pm 6.7$  ms in the control group. These values were much lower than the results presented by Dilaveris, but the growing popularity of the P-wave dispersion theory decreased the meaning of those findings.

The methodology based on automatic software became an inspiration for the study team. The goal was to create an automatic algorithm with the accuracy of measurement comparable to the one reached in manual methodology. Considering the manual methodology, the level of accuracy reached using the properties of vector graphics was 1 pixel – 1 millisecond. The algorithm needed to be able to reflect the skills of an experienced researcher without being any more or less precise. After multiple analyses of the ECG records, it was decided on how to create the algorithm in the expected formula. The main assumption was based on using the properties of vector graphics for the recording of the signal. The ECG graph was formed of the coordinate points filtered every 1 ms. The biggest advantage of vector graphics is the ability of infinite, lossless enlargement of the graphs [14]. Contrary to raster graphics (e.g. a regular ECG paper printout), vector graphics are fully scalable, with no quality loss after changing proportions [15]. The scalable ECG record can adapt its quality to a given resolution, which is very important in making a precise measurement, especially in the case of the P-waves. For example, the structurally damaged atria, as in the case of paroxysmal AF, results in flat and long P-waves, which require higher precision in measurements. Respectively, in the case of less severe arrhythmias, the P-waves are shorter and more distinct. This observation was confirmed by the study results. The issue related to excessively long P-waves results in self-hiding of their actual duration, which was recently described in the work by Mercik et al. [2]. It means that the longer the P-wave is (indicating most probably the interatrial conduction disorders), the more difficult it is to assess its actual duration, despite the technology used, as it was reflected also in the research. To support this statement – the mean difference between automatic and manual measurements was 3.72 ms in all patients, including all P-wave durations. Concluding from this, the described dissimilarities couldn't come from the algorithm, but from the phenomenon of self-hiding, which is a real problem in taking objective measurements. In extreme cases, the P-waves may be long, flat and irregular to such extent, that they may seem to be short while

zooming out. In such cases, the flat and regular parts of the P-waves are averaged to suit the given resolution, and they seem like an integral part of the isoelectric line. In the authors' opinion, this was the case in the study by Nielsen et al. [16]. The authors stated that not only the long duration of the P-wave but also the short one related to the higher risk of AF. Without detailed information on the methodology, one can suspect that the P-waves qualified as "very short" (< 89 ms) were the result of the insufficient precision of measurement. Based on electrophysiological knowledge, a short and regular profile of the P-wave happens in quick and physiological signal conduction, which would be unlikely related to the higher risk of AF. This result is also supported by the numbers obtained in the research. The minimum and maximum P-wave durations are respectively 115–147 ms (automatic measurements), and 115–156 ms (manual measurements). Based on those results in the authors' opinion, in particular in older adults, there is no such category as "very short" P-wave and if some get such measurements of the P-wave duration, this fact requires a more accurate methodology, and that would be an interesting direction of the future research (*Folia Cardiologica*).

To summarize, the APPA algorithm was proven to be practically as accurate in measurements as an experienced researcher using the means of vector graphics. The correct methodology in assessing the P-wave is essential for making the right diagnosis in clinical practice. The determination of the precise P-wave duration as well as the accurate assessment of the P-wave morphology, including interatrial conduction remains the goal for future research. The detailed analysis of these variables potentially increases the chances of determining a new parameter in the prediction of recurrent atrial fibrillation in clinical practice, as the current ones are insufficient.

## Conclusions

The automatic precise P-wave assessment algorithm is comparably accurate in taking the measurements to an experienced researcher.

APPA can be used for scientific purposes to analyse the data saved in the form of coordinates of the signal filtered every 1 ms.

The use of an automatic algorithm doesn't increase the precision of measurements per se, but increasing the number of analysed P-waves per patient, which is the part of algorithm's methodology, makes the final values more reliable.

After increasing the precision of measurements, the differences between minimal and maximal duration of the P-waves in different leads decrease to negligible values.

The structural destruction of atria results in self-hiding of the actual duration of the P-waves in ECG. In clinical practice, it can result in the wrong interpretation of the atrial damage.

### Study limitations

A significant limitation of this study is its innovative nature, so it is impossible to compare the present results in the field of automatic measurement with the results of other authors. Moreover, it is difficult to talk about presenting the software to a wide range of users without the graphic interface which simplifies the use and the analysis in the

unproduced commercial version of the program. The software uses data in the form of coordinates that cannot be obtained from all electrophysiological systems.

### Conflict of interest

The authors have no conflicts of interest to declare. All co-authors have seen and agree with the contents of the manuscript and there is no financial interest to report.

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### Streszczenie

**Wstęp.** Aktywność elektrofizjologiczna serca jest rejestrowana i przedstawiana w postaci elektrokardiogramu (EKG). Precyzyjny pomiar załamka P jest niezbędny do prawidłowej oceny przewodzenia sygnału wewnątrz przedsionków. W celu walidacji precyzyjnych pomiarów manualnych zespół badawczy stworzył automatyczne oprogramowanie dostosowane do precyzyjnych pomiarów fali P (automatyczna precyzyjna ocena załamków P, APPA). Celem niniejszej pracy jest wykazanie, że algorytm automatyczny ma porównywalną skuteczność w precyzyjnym pomiarze czasu trwania załamka P.

**Materiał i metody.** Grupę badaną stanowiło 72 chorych (31 mężczyzn, 41 kobiet) w wieku  $62,8 \pm 14,27$  lat, poddawanych różnym zabiegom elektrofizjologicznym. Załamek P mierzono dwukrotnie: za pierwszym razem ręcznie przy prędkości papieru 200 mm/s, 64–128× (pomiar precyzyjny), a za drugim razem automatycznie przy użyciu systemu APPA, który filtruje sygnał co 1 ms.

**Wyniki.** Nie stwierdzono statystycznych różnic pomiędzy pomiarami ręcznymi i automatycznymi. Średnia różnica pomiędzy tymi dwiema metodami wynosi 3,72 ms. Mediana czasu trwania załamka P była nieznacznie wyższa w przypadku pomiarów manualnych we wszystkich rodzajach arytmii. Największa różnica wystąpiła u pacjentów z migotaniem przedsionków. Najmniejsza różnica występowała w przedziale 110–130 ms czasu trwania załamka P.

**Wnioski.** Pomiary wykonane przez APPA oraz manualnie są równie dokładne, co potwierdza wcześniejsze wyniki uzyskane przez autorów. Algorytm pomiarów charakteryzuje się wysoką wiarygodnością wyników i może być wykorzystywany do celów naukowych. Strukturalne zniszczenie przedsionków prowadzi do samoukrycia rzeczywistego czasu trwania załamków P w EKG. Przy większej precyzji pomiarów różnice pomiędzy minimalnym i maksymalnym czasem trwania załamków P w różnych odprowadzeniach zmniejszają się do wartości pomijalnych.

Słowa kluczowe: czas trwania załamka P, automatyczny algorytm, oprogramowanie, pomiary załamka P

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### References

1. Zimmer K, Przywara W, Zyśko D, et al. The nature of P-wave dispersion – a clinically useful parameter that does not exist. *Int J Cardiol.* 2016; 212: 59–60, doi: [10.1016/j.ijcard.2016.03.031](https://doi.org/10.1016/j.ijcard.2016.03.031), indexed in Pubmed: [27031821](https://pubmed.ncbi.nlm.nih.gov/27031821/).
2. Mercik J, Gajek A, Radziejewska J, et al. The short P-wave – is it really short? *Cardiol J.* 2021; 28(6): 999–1000, doi: [10.5603/CJ.2021.0160](https://doi.org/10.5603/CJ.2021.0160), indexed in Pubmed: [34985126](https://pubmed.ncbi.nlm.nih.gov/34985126/).
3. Chávez-González E, Donoiu I. Utility of P-wave dispersion in the prediction of atrial fibrillation. *Curr Health Sci J.* 2017; 43(1): 5–11, doi: [10.12865/CHSJ.43.01.01](https://doi.org/10.12865/CHSJ.43.01.01), indexed in Pubmed: [30595848](https://pubmed.ncbi.nlm.nih.gov/30595848/).
4. Carmona Puerta R, Lorenzo Martínez E, Rabassa López-Calleja M, et al. Vectorial theory surpasses the local theory in explaining the origin of P-wave dispersion. *J Electrocardiol.* 2021; 66: 152–160, doi: [10.1016/j.jelectrocard.2021.04.015](https://doi.org/10.1016/j.jelectrocard.2021.04.015), indexed in Pubmed: [33962125](https://pubmed.ncbi.nlm.nih.gov/33962125/).
5. Kalton G. Simple random sampling. In: *Introduction to survey sampling.* SAGE Publications Inc 1983.
6. Corlett T. Sampling errors in practice. *Market Research Society Journal.* 2018; 38(4): 1–10, doi: [10.1177/147078539603800402](https://doi.org/10.1177/147078539603800402).
7. Zawadzki J, Zawadzki G, Radziejewska J, et al. The P wave dispersion-one pixel, one millisecond. *Rev Cardiovasc Med.* 2021; 22(4):

- 1633–1640, doi: [10.31083/j.rcm2204170](https://doi.org/10.31083/j.rcm2204170), indexed in Pubmed: [34957805](https://pubmed.ncbi.nlm.nih.gov/34957805/).
8. Zawadzki J, Adamowicz J, Sławuta A, et al. The P wave duration in patients with atrial fibrillation undergoing cryoballoon pulmonary vein isolation. Preliminary results. *Eur J Transl Clin Med*. 2018; 1(1): 42–45, doi: [10.31373/ejtc/96253](https://doi.org/10.31373/ejtc/96253).
  9. Dilaveris PE, Gialafos E, Sideris S, et al. Simple electrocardiographic markers for the prediction of paroxysmal idiopathic atrial fibrillation. *Am Heart J*. 1998; 135(5): 733–738, doi: [10.1016/s0002-8703\(98\)70030-4](https://doi.org/10.1016/s0002-8703(98)70030-4).
  10. Akcay M. The effect of moderate altitude on Tp-e interval, Tp-e/QT, QT, cQT and P-wave dispersion. *J Electrocardiol*. 2018; 51(6): 929–933, doi: [10.1016/j.jelectrocard.2018.07.016](https://doi.org/10.1016/j.jelectrocard.2018.07.016), indexed in Pubmed: [30497749](https://pubmed.ncbi.nlm.nih.gov/30497749/).
  11. Dogan A, Kahraman H, Ozturk M, et al. P wave dispersion and left atrial appendage function for predicting recurrence after conversion of atrial fibrillation and relation of p wave dispersion to appendage function. *Echocardiography*. 2004; 21(6): 523–530, doi: [10.1111/j.0742-2822.2004.03133.x](https://doi.org/10.1111/j.0742-2822.2004.03133.x), indexed in Pubmed: [15298688](https://pubmed.ncbi.nlm.nih.gov/15298688/).
  12. Zawadzki JM, Zimmer K, Przywara W, et al. The true nature of P wave dispersion. *Adv Clin Exp Med*. 2020; 29(12): 1443–1447, doi: [10.17219/acem/128232](https://doi.org/10.17219/acem/128232), indexed in Pubmed: [33389834](https://pubmed.ncbi.nlm.nih.gov/33389834/).
  13. Yamada T, Fukunami M, Shimonagata T, et al. Dispersion of signal-averaged P wave duration on precordial body surface in patients with paroxysmal atrial fibrillation. *Eur Heart J*. 1999; 20(3): 211–220, doi: [10.1053/euhj.1998.1281](https://doi.org/10.1053/euhj.1998.1281), indexed in Pubmed: [10082154](https://pubmed.ncbi.nlm.nih.gov/10082154/).
  14. Fuchs G, Schumann H, Rosenbaum R. Progressive imagery with scalable vector graphics. *SPIE Proceedings*. 2011, doi: [10.1117/12.871935](https://doi.org/10.1117/12.871935).
  15. Rodríguez-López S, Escobedo Martínez MF, Junquera L, et al. Two-dimensional analysis of digital images through vector graphic editors in dentistry: new calibration and analysis protocol based on a scoping review. *Int J Environ Res Public Health*. 2021; 18(9), doi: [10.3390/ijerph18094497](https://doi.org/10.3390/ijerph18094497), indexed in Pubmed: [33922692](https://pubmed.ncbi.nlm.nih.gov/33922692/).
  16. Nielsen JB, Kühl JT, Pietersen A, et al. P-wave duration and the risk of atrial fibrillation: Results from the Copenhagen ECG Study. *Heart Rhythm*. 2015; 12(9): 1887–1895, doi: [10.1016/j.hrthm.2015.04.026](https://doi.org/10.1016/j.hrthm.2015.04.026), indexed in Pubmed: [25916567](https://pubmed.ncbi.nlm.nih.gov/25916567/).